

Comparative Study on MATLAB based Joint Photographic Experts Group Image Size Reduction Using Shearlet and Wavelet Packet Transform for X-ray Images with Potential Hospital Data Storage Applications

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Abstract

Aim: Aim of this study is to compress X-ray images using wavelet packet transform and shearlet transform. These two transforms were compared for the better compression ratio to store large hospital data files in small memory space. Materials and methods: Sample X-ray images were, Wavelet packet (30) and Shearlet (30) for compression. Compression ratio was calculated. The significance of the data were calculated using SPSS software. Results: There was statistical significance between the wavelet packet and shearlet transform based compression ratio data (p<0.05, independent sample t- test). Conclusion: wavelet packet transform has a better compression ratio than shearlet transform. Wavelet packet transform appears to produce the most consistent results with higher standard deviation (3.3) when compared with shearlet transform which appears to produce lower results with lower standard deviation (0.8).

Key-words: Shearlet Transform, X-ray Images, Novel Image Compression Technique, Artificial Intelligence.

1. Introduction

In the current study, we simulated on MATLAB© (2015), it helps to reduce the image size by using wavelet packet and shearlet transform for X-ray images. It stores the data in lower data bytes, hence less transition bandwidth consumed (Subramanian et al., 2010). Here the meaning of bandwidth is to transfer the maximum data across to the point. X-ray is a common imaging test for

the doctors to view internal parts without having any incision on the patient's body. X-rays are passed through the patient's body to detect any tumor formation, bone fractures or any damaged part inside the body. By the compression of image size then it is capable of storing a large amount of files (Dong & Shi, 2008); (Sun Z. & Chang C. C., 2002). We evaluated the better compression ratio generated pertaining to X-ray images while comparing the transforms - wavelet packet transform with shearlet transform. The importance of this study in today's world is to compress the image and reduce the redundancy (Meyer et al., 2000); (Wu & Liu, 2009). The existing experience in my research in MATLAB© coding. We worked on coding for wavelet packet and shearlet transform.

We worked out on the wavelet packet code and shearlet code then we got results as a compressed image. Wavelet packet transform output is sixteen levels of different compressed image formation. It has been reported that wavelet packet is very effective in image processing especially image compression. The shearlet transform output is about restoring the image and finally form it to the compressed size and finally applicable for the hospital data storage (Saleh & Rahman, 2010); (Ghodrati & Asadi, 2009). Large data files can be stored in a small data file due to the compression of the image. The main aim of this study is to compress X-ray using wavelet packet transform and shearlet transform and comparing the transform for better compression ratio (CR). Barro and team found that the use of the wavelet analysis reduced the spectral leakage due to the imperfect frequency response (Barros et al., 2012). Similarly, 24 subband wavelet packet trees approximated to the mean scale frequency division (Degaonkar & Apte, 2013). Hence, throwing light on the fact that the wavelet packet transform provided the same frequency bandwidth in each resolution for recording the feature (Bit rate -17.9) (Mudunuri & Savithri, 2011); (Chang et al., 2010).

Previously our team has a rich experience in working on various research projects across multiple disciplines (Gheena & Ezhilarasan, 2019; Jose et al., 2020; Ke et al., 2019; Krishnaswamy et al., 2020; Malli Sureshbabu et al., 2019; Mehta et al., 2019; Muthukrishnan et al., 2020; M. S. Samuel et al., 2019; S. R. Samuel et al., 2020; Sathish & Karthick, 2020; Sharma et al., 2019; Varghese et al., 2019; Venu, Raju, et al., 2019; Venu, Subramani, et al., 2019; Vignesh et al., 2019; Vijayakumar Jain et al., 2019). Now the growing trend in this area motivated us to pursue this project.

So this motivated us to find a better transform based compression platform exclusively for X-rays as compression for the same has not been reported before. MATLAB© 15 was used to run the programs and get the ratios of compression for both our target transforms.

2. Materials and Methods

In this study, the number of groups were 2. Group 1 had 30 X-ray images compressed using wavelet packet transform. Group 2 had 30 X-ray images compressed using shearlet transform. For the statistical analysis we used SPSS (statistical package for the social sciences). The site for pre test power was calculated from clinical.com using base paper as cited (*Website*, n.d.); (Eben Sophia & Anitha, 2017). This process requires power for about 80% and the value of alpha was 0.05. There were no independent variables. The data collection was done from kaggle dataset [kaggle .com /paultomothymooney chest X-ray pneumonia] (*Kaggle: Your Machine Learning and Data Science Community*, n.d.).

Group 1 Sample images were resized to 512*512 dimension for wavelet packet transform. Basic code for wavelet packet transform that we used z= wprec2(wpdec2(y1,'db1'));. Similarly for shearlet the sample images were processed to the same dimensions with basic code being $z= x_noisy=x+sigma.*radn(L,L)$;. The procedure to use transforming code based simulation with testing setup in MATLAB (2015) was opted in our study. In wavelet packet transform input images were decomposed later it was compressed to form the original image of reduced size. In the same way the shearlet transform directly compresses the original image to form a restored image. The data collection was done from kaggle dataset [kaggle .com /paultomothymooney chest X-ray pneumonia] (*Kaggle: Your Machine Learning and Data Science Community*, n.d.).

Statistical Analysis

SPSS was the statistical software used for analysis. The analysis was done by an independent t- test (p<0.0001). By comparing the output image size by input image size we got the compression ratio. The dependent variable in our study is the compression ratio generated for each image for the respective transforms. Later the ratios were compared.

3. Results

From Table 1, it was observed that the total size of sample for the study was 60. For Wavelet Packet, 30 images and Shearlet 30 were used for the compression process. The original image size ranges from 130 to 450 kb and for shearlet 130 to 198 kb. The compressed image sizes ranged from

26 to 33 kb with the compression ratio on an average of 6 - 12 for Wavelet packet. For Shearlet, the compressed image sizes ranged from 38 to 42 kb with the compression ratio - 3 to 5.5.

S. No	Wavelet packet X- ray original image size (kb)	Wavelet packet X-ray compression image size (kb)	Wavelet packet X-ray compression ratio	Shearlet X- ray original image size (kb)	Shearlet X- ray compression image size (kb)	Shearlet X- ray compression ratio	
1	193	26	7.42	193	40	4.7	
2	193	26.8	7.2	193	40.8	4.7	
3	134	22.1	6.06	134	41.5	3.2	
4	198	28.7	6.89	198	41	4.8	
5	383	26	14.7	150	40.7	3.6	
6	439	27.6	15.9	197	40	3.6	
7	379	28.1	13.4	154	39.5	4.9	
8	447	28.6	15.6	211	39.5	3.8	
9	354	28.6	12.3	139	39	5.3	
10	427	31.4	13.5	193	40.2	3.5	
11	359	24.2	14.8	134	39.5	4.8	
12	427	29.5	14.4	190	39.4	3.3	
13	415	30.2	13.7	190	38.8	4.8	
14	413	29.6	13.9	183	40.2	4.8	
15	411	28.6	14.3	180	40.5	4.5	
16	411	32.4	12.6	185	38.7	4.4	
17	417	31.6	13.19	185	39.7	4.7	
18	407	32.5	12.5	188	39.1	4.6	
19	335	25	13.4	121	40.3	4.8	
20	392	31.2	12.5	179	40.8	3	
21	358	28.7	12.8	144	39	4.38	
22	353	26.3	13.4	135	39	3.6	
23	330	26.1	12.6	125	38.9	3.46	
24	345	23.6	14.6	122	39.7	3.21	
25	345	23.6	14.6	122	39.9	3.07	
26	441	32.6	13.5	211	39.8	3.05	
27	348	22.4	15.5	122	39.5	5.3	
28	328	21.4	15.3	110	40.2	3	
29	345	23.6	14.6	122	40.3	2.7	
30	375	28.7	13	153	40.4	3	

Table 1- Represents the Total Sample Size Used in the Compression Study

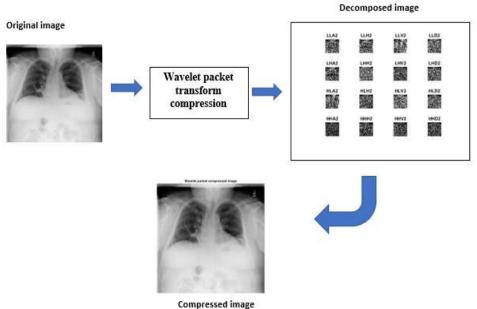


Fig. 1- Represents the Wavelet Packet Transform Compression of X- ray Images

Figure 1 represents the wavelet packet transform compression of X-ray images. 30 images were compressed to obtain compression ratios. The transform decomposes the input image to 16 subsets to reduce noise and finally recontructs it while compressing simultaneously. Hence, images with reduced sizes are generated. Similarly, Fig. 2 represents the shearlet transform compression of X-ray images. X-ray images were pre-processed first for the bit rate of the images according to the code. They were directly compressed and later restored to have output images of reduced sizes. From Table 2, represents the group statistics data for this study. Wavelet packet based compression ratio was seen to be higher with mean value of 13.53, when compared to that of shearlet.

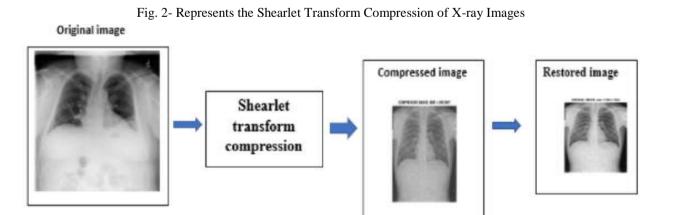


 Table 2- Represents the Group Statistics Data for this Study. Wavelet Packet based Compression Ratio was seen to be Higher with Mean value of 13.53 when compared to that of Shearlet

	Group	Ν	Mean	Std. Deviation	Std. Error Mean
aamn natio	Wavelet Packet	30	13.5377	3.35491	0.61252
comp_ratio	Shearlet	30	4.0257	0.8044	0.14686

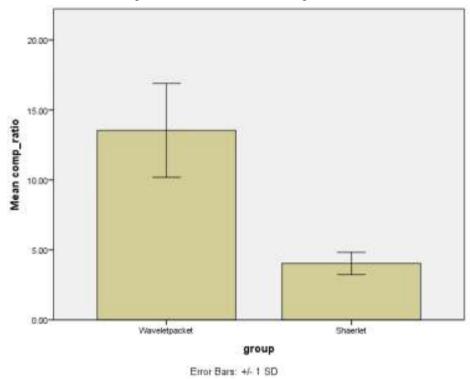
Table 3 depicts the comparison of wavelet packet based compression ratio with shearlet transform based compression ratio for 30 X-ray images. The wavelet packet transform had the highest compression ratio with the mean value of 13.53, when compared with the shearlet transform which had a lowest compression ratio with the mean value of 4.02. It was a statistically significant study with p value of 0.032. Hence supporting our hypothesis and our experimental results.

Table 3- Represents the Result of an Independent Sample t Test, for Wavelet Packet based Compression Ratio of Mammographic Image. There was a Statistical Significance between DCT and Shearlet Data (p=0.035) (p<0.05 Independent Sample t Test)

		-		t-test for Equality of Means						
		F	Sig.	t	df	Sig. (2- tailed)	Mean Difference	Std. Error Difference	95% Con Interval Differen Lower	of the
	Equal variances assumed	4.8	0.032	15.1	58	0	9.512	0.62988	8.251	10.7728
comp_ratio	Equal variances not assumed			15.1	32.3	0	9.512	0.62988	8.229	10.7945

Figure 3 reports the comparison between wavelet packet and shearlet transform compression ratio for X-ray images. There was statistical significance between the data (p<0.05, independent sample t- test). Wavelet packet transform appears to produce the most consistent results with higher standard deviation (3.3) when compared with shearlet transform, which appears to produce lower results with lower standard deviation (0.8). Since the deviation is more for shearlet when compared to Wavelet Packet, the former has a prospects of upgrading its compression features if optimized aptly.

Fig. 3- Comparison between Wavelet Packet and Shearlet Transform Compression Ratio for x- ray Images. Wavelet Packet Transform appears to Produce the most Consistent Results with Higher Standard Deviation (3.3) when compared with Shearlet Transform which appears to Produce Lower Results with Lower Standard Deviation (0.8). X Axis: Wavelet packet vs Shearlet Transform Group. Y Axis: Mean Value of Compression Ratio +/- 1 SD



4. Discussion

Wavelet packet transform with higher standard deviation (3.3) has the potential for upgradation and enhancement of compression parameters (p=0.032, p<0.05 independent sample t test). CR for wavelet packet transform was seen to be higher (13.53) than its counterpart. Hence seems to be a better transform for compressing X-ray images. So the wavelet packet transform is better than shearlet transform for X-ray images.

Previously it has been suggested that wavelet packet is a novel algorithm for differential protection of three phase power transformers (Rahman & Al Mehedi Hasan, 2014). Similarly in 2017 scientists have reported that applications in X- ray using wireless technology was very predominant in the health industry (Al-Busaidi et al., 2017); (Subramanian et al., 2010). It has been suggested that secure and robust host, adapted color image watermarking using inter layered wavelet packets is very efficient (Meyer et al., 2000); (Al-Otum, 2019). As the efficiency of the transforms are good enough for most of the image formats, there were no negative reports that we could cite for the same. From the above reports, we inferred that various transforms are very frequently used in image compression

but none of them have been compared based on their compression ratios and used exclusively for medical images. So our study helps to find out the most suitable transform with better compression ratio pertaining to X-ray images. The use of shearlet as a compression transform for X-ray images is the novelty of this study. Hence wavelet packet transform is suggested to be better than shearlet transform for X-ray images.

Our institution is passionate about high quality evidence based research and has excelled in various fields ((Ezhilarasan et al., 2019; Mathew et al., 2020; Pc et al., 2018; Ramadurai et al., 2019; Ramesh et al., 2018; Sridharan et al., 2019; Vijayashree Priyadharsini, 2019). We hope this study adds to this rich legacy.

Pre-processing of images before the compression (based on the code) is our major limitation. If the code is optimized to perform compression for every image regardless of size type and dimension (Subramanian et al., 2010) will be more effective.

The future prospect of this study is to come up with better code for better compression to store the large data files in a small file.

5. Conclusion

In this study, wavelet packet transform has a better compression ratio than shearlet transform. Wavelet packet transform appears to produce the most consistent results with higher standard deviation (3.3) when compared with shearlet transform which appears to produce lower results with lower standard deviation (0.8) when analysed using independent t test. The higher standard deviation gives wavelet packet transform more potential for upgradation and enhancement of compression parameters. Hence seems to be a better transform for compressing X- ray images.

Declarations

Conflict of Interests

No conflict of interest in this manuscript.

Authors Contributions

Author PH was involved in compression of images data analysis and manuscript writing, Author ND was involved in conceptualization, data validation and critical review of manuscript.

Acknowledgements

The authors would like to express their gratitude to the Saveetha School of Engineering, Saveetha Institute of Medical and Technical Sciences (formerly known as Saveetha University) for providing the necessary infrastructure to carry out this work successfully.

Funding's

We thank the following organizations for providing financial support that enabled us to complete the study.

- 1. Sri chakra consultants.
- 2. Saveetha University
- 3. Saveetha Institute of Medical and Technical Sciences
- 4. Saveetha School of Engineering.

References

Al-Busaidi, A.M., Khriji, L., Touati, F., Rasid, M.F., & Mnaouer, A.B. (2017). Wavelet-based Encoding Scheme for Controlling Size of Compressed ECG Segments in Telecardiology Systems. *Journal of Medical Systems*, *41*(10), 166.

Al-Otum, H.M. (2019). Image watermarking based on inter-tree coefficients differencing in paired wavelet-packets tree constructions. In *Multimedia Tools and Applications*, 78(16), 22909–22937. https://doi.org/10.1007/s11042-019-7542-3

Barros, J., Diego, R.I., & De Apraiz, M. (2012). Applications of Wavelet Transform for Analysis of Harmonic Distortion in Power Systems: A Review. *In IEEE Transactions on Instrumentation and Measurement* (Vol. 61, Issue 10, pp. 2604–2611). https://doi.org/10.1109/tim.2012.2199194

Chang, F., Hong, W., Zhang, T., Jing, J., & Liu, X. (2010). Research on Wavelet Denoising for Pulse Signal Based on Improved Wavelet Thresholding. In 2010 First International Conference on Pervasive Computing, Signal Processing and Applications. https://doi.org/10.1109/pcspa.2010.142

Degaonkar, V.N., & Apte, S.D. (2013). Emotion modeling from speech signal based on wavelet packet transform. *International Journal of Speech Technology*, *16*(1), 1–5.

Dong, X., & Shi, S. (2008). Identifying Single-Phase-to-Ground Fault Feeder in Neutral Noneffectively Grounded Distribution System Using Wavelet Transform. *IEEE Transactions on Power Delivery*, 23(4), 1829–1837.

Eben Sophia, P., & Anitha, J. (2017). Contextual Medical Image Compression using Normalized Wavelet-Transform Coefficients and Prediction. *IETE Journal of Research*, 63(5), 671–683.

Ezhilarasan, D., Apoorva, V.S., & Ashok Vardhan, N. (2019). Syzygium cumini extract induced reactive oxygen species-mediated apoptosis in human oral squamous carcinoma cells. *Journal of Oral Pathology & Medicine: Official Publication of the International Association of Oral Pathologists and the American Academy of Oral Pathology*, 48(2), 115–121.

Gheena, S., & Ezhilarasan, D. (2019). Syringic acid triggers reactive oxygen species-mediated cytotoxicity in HepG2 cells. *Human & Experimental Toxicology*, *38*(6), 694–702.

Ghodrati, A.G., & Asadi, A. (2009). Comparison of different methods of wavelet and wavelet packet transform in processing ground motion records.

https://www.sid.ir/en/journal/ViewPaper.aspx?ID=166132

Jose, J., Ajitha, & Subbaiyan, H. (2020). Different treatment modalities followed by dental practitioners for Ellis class 2 fracture – A questionnaire-based survey. *The Open Dentistry Journal*, 14(1), 59–65.

Kaggle: Your Machine Learning and Data Science Community. (n.d.). Retrieved March 17, 2021, from https://www.kaggle.com/

Ke, Y., Al Aboody, M.S., Alturaiki, W., Alsagaby, S.A., Alfaiz, F.A., Veeraraghavan, V.P., & Mickymaray, S. (2019). Photosynthesized gold nanoparticles from Catharanthus roseus induces caspase-mediated apoptosis in cervical cancer cells (HeLa). *Artificial Cells, Nanomedicine, and Biotechnology*, *47*(1), 1938–1946.

Krishnaswamy, H., Muthukrishnan, S., Thanikodi, S., Arockiaraj, G., Antony, & Venkatraman, V. (2020). Investigation of air conditioning temperature variation by modifying the structure of passenger car using computational fluid dynamics. *Thermal Science*, *24*(1 Part B), 495–498.

Malli Sureshbabu, N., Selvarasu, K., V, J.K., Nandakumar, M., & Selvam, D. (2019). Concentrated Growth Factors as an Ingenious Biomaterial in Regeneration of Bony Defects after Periapical Surgery: A Report of Two Cases. *Case Reports in Dentistry*, 2019, 7046203.

Mathew, M.G., Samuel, S.R., Soni, A.J., & Roopa, K.B. (2020). Evaluation of adhesion of Streptococcus mutans, plaque accumulation on zirconia and stainlesssteel crowns, and surrounding gingival inflammation in primary. *Clinical Oral Investigations*.

https://link.springer.com/article/10.1007/s00784-020-03204-9

Mehta, M., Deeksha, Tewari, D., Gupta, G., Awasthi, R., Singh, H., Pandey, P., Chellappan, D.K., Wadhwa, R., Collet, T., Hansbro, P.M., Kumar, S.R., Thangavelu, L., Negi, P., Dua, K., & Satija, S. (2019). Oligonucleotide therapy: An emerging focus area for drug delivery in chronic inflammatory respiratory diseases. *Chemico-Biological Interactions*, *308*, 206–215.

Meyer, F.G., Averbuch, A.Z., & Strömberg, J.O. (2000). Fast adaptive wavelet packet image compression. *IEEE Transactions on Image Processing: A Publication of the IEEE Signal Processing Society*, *9*(5), 792–800.

Mudunuri, S.P., & Savithri, S.P. (2011). A Novel Adaptive Audio Watermarking using a Random Waveletpacket Tree and Singular Value Decomposition. *In Signal and Image Processing and Applications / 716: Artificial Intelligence and Soft Computing*.

https://doi.org/10.2316/p.2011.738-057

Muthukrishnan, S., Krishnaswamy, H., Thanikodi, S., Sundaresan, D., & Venkatraman, V. (2020). Support vector machine for modelling and simulation of heat exchangers. *Thermal Science*, *24* (1 Part B), 499–503.

Pc, J., Marimuthu, T., & Devadoss, P. (2018). Prevalence and measurement of anterior loop of the mandibular canal using CBCT: A cross sectional study. *Clinical Implant Dentistry and Related Research*. https://europepmc.org/article/med/29624863

Rahman, M.J., & Al Mehedi Hasan, M. (2014). Performance of Wavelet Transform on Models in Forecasting Climatic Variables. *In Computational Intelligence Techniques in Earth and Environmental Sciences*, 141–154. https://doi.org/10.1007/978-94-017-8642-3_8

Ramadurai, N., Gurunathan, D., Samuel, A.V., Subramanian, E., & Rodrigues, S.J.L. (2019). Effectiveness of 2% Articaine as an anesthetic agent in children: randomized controlled trial. *Clinical Oral Investigations*, *23*(9), 3543–3550.

Ramesh, A., Varghese, S., Jayakumar, N.D., & Malaiappan, S. (2018). Comparative estimation of sulfiredoxin levels between chronic periodontitis and healthy patients - A case-control study. *Journal of Periodontology*, 89(10), 1241–1248.

Saleh, S.A., & Rahman, M.A. (2010). Testing of a Wavelet-Packet-Transform-Based Differential Protection for Resistance-Grounded Three-Phase Transformers. *IEEE Transactions on Industry Applications*, *46*(3), 1109–1117.

Samuel, M.S., Bhattacharya, J., Raj, S., Santhanam, N., Singh, H., & Pradeep Singh, N.D. (2019). Efficient removal of Chromium(VI) from aqueous solution using chitosan grafted graphene oxide (CS-GO) nanocomposite. *International Journal of Biological Macromolecules*, *121*, 285–292.

Samuel, S.R., Acharya, S., & Rao, J.C. (2020). School Interventions-based Prevention of Early-Childhood Caries among 3-5-year-old children from very low socioeconomic status: Two-year randomized trial. *Journal of Public Health Dentistry*, 80(1), 51–60.

Sathish, T., & Karthick, S. (2020). Wear behaviour analysis on aluminium alloy 7050 with reinforced SiC through taguchi approach. *Journal of Japan Research Institute for Advanced Copper-Base Materials and Technologies*, 9(3), 3481–3487.

Sharma, P., Mehta, M., Dhanjal, D.S., Kaur, S., Gupta, G., Singh, H., Thangavelu, L., Rajeshkumar, S., Tambuwala, M., Bakshi, H.A., Chellappan, D.K., Dua, K., & Satija, S. (2019). Emerging trends in the novel drug delivery approaches for the treatment of lung cancer. *Chemico-Biological Interactions*, *309*, 108720.

Sridharan, G., Ramani, P., Patankar, S., & Vijayaraghavan, R. (2019). Evaluation of salivary metabolomics in oral leukoplakia and oral squamous cell carcinoma. *Journal of Oral Pathology & Medicine: Official Publication of the International Association of Oral Pathologists and the American Academy of Oral Pathology*, 48(4), 299–306.

Subramanian, S., Mathur, B., & Henry, J. (2010). Wavelet packet transform and support vector machine based discrimination of power transformer inrush current from internal fault currents. *Modern Applied Science*, *4*(5). https://doi.org/10.5539/mas.v4n5p67

Sun Z., & Chang C.C. (2002). Structural Damage Assessment Based on Wavelet Packet Transform. *Journal of Structural Engineering*, *128*(10), 1354–1361.

Varghese, S.S., Ramesh, A., & Veeraiyan, D.N. (2019). Blended Module-Based Teaching in Biostatistics and Research Methodology: A Retrospective Study with Postgraduate Dental Students. *Journal of Dental Education*, 83(4), 445–450.

Venu, H., Raju, V.D., & Subramani, L. (2019). Combined effect of influence of nano additives, combustion chamber geometry and injection timing in a DI diesel engine fuelled with ternary (diesel-biodiesel-ethanol) blends. *Energy*, *174*, 386–406.

Venu, H., Subramani, L., & Raju, V.D. (2019). Emission reduction in a DI diesel engine using exhaust gas recirculation (EGR) of palm biodiesel blended with TiO2 nano additives. *Renewable Energy*, *140*, 245–263.

Vignesh, R., Sharmin, D., Rekha, C.V., Annamalai, S., & Baghkomeh, P.N. (2019). Management of Complicated Crown-Root Fracture by Extra-Oral Fragment Reattachment and Intentional Reimplantation with 2 Years Review. *Contemporary Clinical Dentistry*, *10*(2), 397–401.

Vijayakumar Jain, S., Muthusekhar, M.R., Baig, M.F., Senthilnathan, P., Loganathan, S., Abdul Wahab, P. U., Madhulakshmi, M., & Vohra, Y. (2019). Evaluation of Three-Dimensional Changes in Pharyngeal Airway Following Isolated Lefort One Osteotomy for the Correction of Vertical Maxillary Excess: A Prospective Study. *Journal of Maxillofacial and Oral Surgery*, *18*(1), 139–146.

Priyadharsini, J.V. (2019). In silico validation of the non-antibiotic drugs acetaminophen and ibuprofen as antibacterial agents against red complex pathogens. *Journal of Periodontology*, 90(12), 1441–1448.

Wu, J.D., & Liu, C.H. (2009). An expert system for fault diagnosis in internal combustion engines using wavelet packet transform and neural network. *Expert Systems with Applications*, *36*(3, Part 1), 4278–4286.